The Eurocrypt 2009 Evaluation Framework for SCAs, Revisited

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Outline

- The big picture
- Motivating worst case evaluation
- Applying the framework
 - Information theoretic analysis
 - Introduction
 - In practice
 - Main theorem
 - Examples of applications
 - Security analysis
- Which statistical tools to use?
- Conclusion



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SCA evaluation framework [1]



Three main ingredients : *design* (e.g. AES in a μ controller), *leakage function* (e.g. power cons. + scope), *adversary*

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Definition of the adversary

- Adv(p, d, n, t, m, s)
 - p : profiled or non-profiled attack
 - d : data complexity (excludes repetition)
 - n : number of measurements (includes repetition)
 - t : time complexity
 - m : memory complexity
 - ► *s* ∈ unknown/known/chosen plaintexts/ciphertexts





Definition of the leakage function

- Formally, $L(\delta, \Sigma, \rho)$
 - $\blacktriangleright~\delta$: configuration of the target device
 - Depends on the public input x and secret input k
 - ▶ May depend on a random (non-physical) parameter *r*
 - Σ : measurement setup
 - ρ : physical randomness





Definition of the leakage function

- Formally, $L(\delta, \Sigma, \rho)$
 - δ : configuration of the target device
 - Depends on the public input x and secret input k
 - ▶ May depend on a random (non-physical) parameter *r*
 - Σ : measurement setup
 - ρ : physical randomness
- Additional informal classification :
 - Independent noise : if $L(x, k, \rho) = f(x, k) + g(\rho)$
 - Variability : if $L(x, k, \rho)$ is different for "similar" chips
 - Linear : if f(x, k) is a linear function of x, k
 - Non-linear : if f(x, k) is a non-linear function of x, k



Specification of the design

- Cryptographic algorithm
- Target device and technology
- Type of countermeasures inserted, e.g.
 - Noise addition
 - Masking
 - Time randomization
 - Dual-rail logic styles
 - Re-keying
 - ▶ ...



Message #1

- SCA depend on many parameters
- Any comparison should fix all of them but one
- e.g. impact of a countermeasure
 - Best analyzed on the same device & with the same setup as the unprotected implementation





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How not to evaluate

Launch a single attack with an arbitrary distinguisher







How not to evaluate

Launch a single attack with an arbitrary distinguisher



First issue : no statistical confidence in the evaluation





A first improvement

Repeat the attack and estimate a success rate







A first improvement

Repeat the attack and estimate a success rate



Second issue : arbitrary adversary (maybe suboptimal)





A first improvement

Repeat the attack and estimate a success rate



A stronger adversary may invalidate the evaluation





A second improvement

Apply an "optimal" template attack







Message #2

- Worst case evaluation
 - Anticipates "all" side-channel adversaries
 - Adds security margins to the implementations
 - Practical adversaries may be suboptimal
 - Represents the designer's point of view
- Profiling is (provably) needed for this purpose [2]





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The starting point

- Why do we need it?
 - All the quantified data of a worst case evaluation is contained in security metrics (e.g. success rates)







The starting point

• Why do we need it?

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 All the quantified data of a worst case evaluation is contained in security metrics (e.g. success rates)



- $\bullet \ \ \mathsf{But evaluating} = \mathsf{quantifying} + \mathsf{understanding}$
- Remaining issue : why is the attack successful ?
 - Information theoretic analysis helps understanding





Estimation issues

- ► Information theoretic analysis = estimating the information leakage ⊥ of the adversary
- But estimating the mutual information between arbitrary distributions is notoriously hard
 - Estimators are biased & distribution-dependent





Estimation issues

- ► Information theoretic analysis = estimating the information leakage ⊥ of the adversary
- But estimating the mutual information between arbitrary distributions is notoriously hard
 - Estimators are biased & distribution-dependent
- ► Good news : side-channel attacks need a model
 - i.e. an estimation of the leakage distribution
- Main idea : estimate the mutual information from the "best available" profiled model (i.e. the worst case)



Definition

Information leakage on the secret key

$$\mathsf{H}[\mathcal{K}] - \sum_{k \in \mathcal{K}} \mathsf{Pr}[k] \sum_{l \in \mathcal{L}} \mathsf{Pr}_{\mathsf{chip}}[l|k] \cdot \log_2 \hat{\mathsf{Pr}}_{\mathsf{model}}[k|l],$$





Definition

- ► Information leakage on the secret key $H[K] - \sum_{k \in \mathcal{K}} \Pr[k] \sum_{l \in \mathcal{L}} \Pr_{chip}[l|k] \cdot \log_2 \hat{\Pr}_{model}[k|l],$
- where $\hat{\Pr}_{model}[k|l]$ is obtained by profiling the target device
- where $\Pr_{\text{chip}}[k|I]$ is obtained by sampling the target device

 \Rightarrow Two cases can happen





Case #1 : ideal evaluation



$\hat{\mathsf{MI}}(K; L) = \mathsf{H}[K] - \sum_{k \in \mathcal{K}} \mathsf{Pr}[k] \sum_{l \in \mathcal{L}} \mathsf{Pr}_{\mathtt{chip}}[l|k] \log_2 \hat{\mathsf{Pr}}_{\mathtt{model}}[k|l]$

\Rightarrow mutual information properly estimated





Case #2 : "biased" evaluation



$$\hat{\mathbb{M}}(K; L) = \mathbb{H}[K] - \sum_{k \in \mathcal{X}} \Pr[k] \sum_{l \in \mathcal{L}} \Pr_{\mathtt{chip}}[l|k] \log_2 \hat{\Pr}_{\mathtt{model}}[k|l]$$
$$\hat{\mathbb{P}}I$$

perceived information = estimator for the mutual information biased by the adversary's model





Message #3

- In general, MI(K; L) cannot be exactly computed
- But we can sometime be sufficiently close
 - (see the "tools" section)
- Goal of an evaluator : be as close as possible
 - Again motivates the use of profiling





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Two-step process

- Step 1 : estimate the leakage model Pr_{model}[k|I]
 - e.g. with Gaussian templates, linear regression [3] (or Gaussian Mixtures, SVMs, ...)
- Step 2 : estimate $\hat{PI}(K; L)$ by sampling $\hat{Pr}_{chip}[k|I]$
 - i.e. by generating actual measurements





Two-step process

- Step 1 : estimate the leakage model Pr_{model}[k|I]
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 - i.e. by generating actual measurements

Note : measurements to estimate the leakage model and to estimate Pl(K; L) must be different



- 4 key candidates with correct key k = 1
- $\sum_{l \in \mathcal{L}} \Pr_{\text{chip}}[l|k=1] \log_2 \hat{\Pr}_{\text{model}}[k=1|l]$ estimation





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$$\begin{array}{ccccccc} k = 0 & k = 1 & k = 2 & k = 3 \\ l_1 & \hat{p}_0^1 & \hat{p}_1^1 & \hat{p}_2^1 & \hat{p}_3^1 \\ l_2 & \hat{p}_0^2 & \hat{p}_1^2 & \hat{p}_2^2 & \hat{p}_3^2 \end{array}$$





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$$l_1 \qquad \hat{p}_0^1 \qquad \hat{p}_1^1 \qquad \hat{p}_2^1 \qquad \hat{p}_3^1$$

$$l_2 \qquad \hat{p}_0^2 \qquad \hat{p}_1^2 \qquad \hat{p}_2^2 \qquad \hat{p}_3^2$$

$$l_3 \qquad \hat{p}_0^3 \qquad \hat{p}_1^3 \qquad \hat{p}_2^3 \qquad \hat{p}_3^3$$

$$\dots \qquad \dots \qquad \dots \qquad \dots \qquad \dots$$

$$l_N \qquad \hat{p}_0^N \qquad \hat{p}_1^N \qquad \hat{p}_2^N \qquad \hat{p}_3^N$$

$$\Rightarrow \frac{1}{N} \sum_{i=1}^N \log_2 \hat{p}_i^i$$



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- MIA requires to define a *target operation*
- MI/PI metrics are best estimated when capturing the key leakage from *all intermediate computations* [5]





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- MIA is a non-profiled distinguisher
- ▶ MI/PI metrics are *profiled* (worst case) eval. criteria
- MIA requires to define a *target operation*
- MI/PI metrics are best estimated when capturing the key leakage from *all intermediate computations* [5]
- The MIA distinguisher provides a lower bound of the actual information leakage given by the MI/PI metrics



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Main theorem (informal)

- PI(K; L) is directly proportional to the success rate of an adversary using Pr_{model}[k|I] as template
- e.g. PI(K; L) in function of the noise variance







As a result

Left of the intersection



• Countermeasure #2 more secure than first one





As a result

Right of the intersection



• Countermeasure #1 more secure than first one





In other words

• MI(K; L) measures the worst case data complexity







In other words

PI(K; L) is the evaluator's best estimate







Relation with data complexity



Theorem only proven in very specific cases





Relation with data complexity



Theorem only proven in very specific cases

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But holds surprisingly well in all real-world settings



Message #4

- A single success rate curve does not reveal a trend nor an explanation about a leaking device
- Most intuition regarding the data complexity of of a side-channel attack can be extracted by plotting PI(K; L) in function of a noise variable
- PI(K; L) curves are easier to sample than the average data complexity to reach a given success rate





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Example #1 : masking

- Main idea : split the sensitive data in r shares
- If "perfect" implementation, the data complexity to break masking is proportional to (σ²_n)^r
 - ▶ Perfect ≈ if the smallest-order key-dependent moment in the leakage distribution is r
 - Essentially depends on the hardware (e.g. glitches or early propagation make implementations imperfect)





Information theoretic intuition [6]



▶ Smallest-order key-dept. moment = slope of the curve



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Information theoretic intuition [6]



Flaws due to physical defaults can be detected



Example #2 : time randomization

- Random delays, unstable clock, shuffling, ...
- Essentially adds noise to the implementation





Information theoretic intuition [7]



e.g. shuffling can give rise to a Y-axis shift



Information theoretic intuition [7]



Main issue : highly dependent on signal processing



Example #3 : dual rail logic styles

- Main idea : have constant activity within the implementation in order to
 - 1. Modify the leakage models (i.e. avoid simple models such as Hamming weight/distance)
 - 2. Reduce the data dependencies in the leakages
- Practical limitation : usually implies strong hardware constraints (i.e. need to "balance" the wires)



Information theoretic intuition [8]



• Reduced data dependencies \Rightarrow X-axis shift



Example #4 : *variability*

- Leakage function can be \neq for \neq "similar" chips
 - ▶ e.g. because of manufacturing process
- Raises new questions regarding profiled attacks
 - e.g. profile *n* chips, attack another chip
 - How large should *n* be?
- Variability may create a gap between MI and PI





Information theoretic intuition [9]



- Worst case may be harder to exploit by adversaries...
- ... but remains the most reliable evaluation metric !

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Message #5

- PI(K; I) provides a unifying view of countermeasures
- Only masking can lead to exponential security increase
- Again, beware of "false sense of security"
 - $PI(K; L) \neq MI(K; L)$
 - Significant differences may be due to signal processing, bad assumptions on the leakage, ...
 - Measurement setup also matters (a lot)





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The starting point

- Why do we need it?
 - Information theoretic curves capture most intuition about the data complexity of worst-case attacks







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- Why do we need it?
 - Information theoretic curves capture most intuition about the data complexity of worst-case attacks



- But side-channel attacks also depend on time
- And evaluating multiple (not only worst-case) adversaries may be revealing as well [10]



Example #1 : masking

 If the r shares are manipulated in different clock cycles (i.e. in software, typically), finding these cycles requires testing N^r r-uples of time samples





Example #2 : key enumeration [11]



Significant impact on the success rates



Example #2 : key enumeration [11]



Missing data can always be traded for computations

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Example #3 : other attacks



Non-profiled attacks can be significantly less efficient



Message #6

- Security analysis : necessary complement to IT analysis
- It allows highlighting the gap between profiled and (usually more realistic) non-profiled attacks
- It incorporates time complexity in the evaluations
 - ► Adversaries can enumerate up to 2⁵⁰-2⁶⁰ keys
 - Evaluate success rates of high orders !





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How to evaluate the metrics?

- Implies to determine good statistical tools
 - Critical point : pdf estimation problem
- Tools are highly dependent on the contexts
- A few examples next...





Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
masking		
combination of countermeasures		

- Different types of implementations & countermeasures
- ▶ Which cases are "easy to evaluate?"



Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
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combination of countermeasures		

- Most distinguishers are asymptotically equivalent
- ... if provided with the same leakage model [12]


Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
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combination of countermeasures		

- ▶ PCA, LDA, ... useful in the profiled case
- Dimensionality reduction uneasy in non-profiled case



Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
masking		
combination of countermeasures		

- Same tools as for an unprotected device
- Non-linear leakage functions require profiling



Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
masking		
combination of countermeasures		

- Uneasy to evaluate for both types of attacks
- Signal proc. completely removes some countermeasures



Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
masking		
combination of countermeasures		

- Becomes measurement intensive as r increases
- No solution is always optimal in the non-profiled case



Examples

	profiled attacks	non-profiled attacks
unprotected device, univariate leakage		
unprotected device, multivariate leakage		
dual-rail pre-charged implementation		
time randomizations		
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combination of countermeasures		

- Specially hard if the design is unknown
- Large distance btw. profiled & non-profiled cases



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Conclusions (I)

- Evaluation of DPA quite well understood in theory
 - Which metrics to use and why
 - Perceived information quantifies implementations
 - Success rates quantify adversaries
- ► But ∃ many open question related to the best statistical tools needed to estimate the metrics





Conclusions (II)

- Evaluators should always try to understand from where a "false sense of security" could come from
 - Perceived information can also be used to compare different laboratories (i.e. how good are they in extracting information from an implementation?)





Conclusions (III)

- Side-channel attacks are more than divide-and-conquer
- Next challenge : combinations with cryptanalysis
 - Collision attacks
 - Algebraic attacks
 - ▶ ...





THANKS

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Evaluation of Side-Channel Attacks - Summer 2012



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