# Towards Leakage-Resistant Post-Quantum CCA-Secure Public Key Encryption







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- Introduction/motivation
  - Parallel with symmetric crypto
  - Challenge for PQ crypto
- POLKA's main design tweaks
  - Rigidity without FO-transform
  - Dummy ciphertext (⇒ leveled implementations)
  - Hard physical learning problems
- Conclusions & open problems

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#### Symmetric crypto (20 years ago)



- CTR mode: uniform protection against DPA
- AES: expensive countermeasures (e.g., masking)

(Vocabulary: DPA = key/state recovery attack with many side-channel traces)

### Symmetric crypto (nowadays)



- Leakage-resistant mode of operation
  - Leveled implementations (mixing expensive DPA protections for a few blocks a cheaper SPA protections)
- Lightweight (easier to protect) block ciphers

(Vocabulary: SPA = key/state recovery attack with a few side-channel traces)

#### Impact can be massive!



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#### PQ encryption (FO-calypse)



- Decryption & re-encryption before the test
- Allows "state comparison" attacks
  - Just distinguishing L(p) from L(cp) leaks about sk
- Even more expensive to prevent than DPA
  - Factor of overheads: 6, 16, 50 for 2, 4 & 8 shares!

top-down: from abstract models to implementations

Can we design quantum-safe CCA-secure encryption schemes that are (much) cheaper to protect against leakage?

(& a bit less efficient if leakage is not a concern)

bottom-up: from heuristic tweaks to formal proofs

Needs humility: completely connecting top-down and bottom-up approaches remains a challenge after 20 years in symmetric crypto

- Remove the state comparison attack path
   ≈ Avoid the FO-transform and leverage rigidity
- 2. Enable leveled implementations
   ≈ Use dummy ciphertexts & ephemeral secrets so that not all intermediate computations are DPA targets
- 3. Make the remaining DPA targets easier to mask ≈ leverage key-homomorphic computations and the (admittedly provocative) hard physical learning problems
- Focusing on key security (leakage-resilience) and not message security (leakage-resistance)

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# POLKA

#### **PO**st-quantum Leakage-resilient public Key encryption Algorithm

- CCA-secure in the QROM (w/o leakage)
- Hybrid encryption with an LPR-like KEM

$$c_1 = a \cdot r + e_1$$
  

$$c_2 = b \cdot r + e_2$$
  
small  $r, e_1, e_2 \leftarrow D$ 

Then,  $K = H(r, e_1, e_2)$  and  $c_0 = AEnc_K(m)$ 

- Rigidity w/o FO + explicit rejection
- Partially randomized decapsulation

#### Base scheme + rigidity

- KeyGen(pp):  $a \leftarrow R_q = F_q[x]/(x^n + 1)$  $b = p \cdot (a \cdot s + e) \in R_q^*$  medium
- Encrypt<sub>a,b</sub>(m):  $c_1 = a \cdot r + e_1$  $c_2 = b \cdot r + e_2$  small  $r, e_1, e_2 \leftarrow D$

Then, 
$$K = H(r, e_1, e_2)$$
 and  $c_0 = AEnc_K(m)$ 

- Decrypt<sub>s</sub>(c):  $c_2 p \cdot c_1 \cdot s = p \cdot (er e_1 s) + e_2$ 
  - ⇒ Extract  $e_2$ , then r, and then  $e_1$ Check if they are small, else abort  $K = H(r, e_1, e_2)$  and  $c_0 = ADec_K(c_0)$

#### Base scheme + rigidity

- KeyGen(pp):  $a \leftarrow R_a = F_a[x]/(x^n + 1)$  $b = p \cdot (a \cdot s + e) \in R_a^*$  medium Encr If extracted  $r, e_1, e_2$  are small,  $P_1, e_2 \leftarrow D$ computing  $a \cdot r + e_1$  and  $b \cdot r + e_2$ would lead to  $c_1$  and  $c_2$ Then But we do not have to do it!  $e_1 s) + e_2$  $(\neq$  FO-transform) Decr
  - ⇒ Extract  $e_2$ , then r, and then  $e_1$ Check if they are small, else abort  $K = H(r, e_1, e_2)$  and  $c_0 = ADec_K(c_0)$

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Decrypt with dummy ciphertext (I)

• Encapsulation is almost homomorphic

$$c_{1} = a \cdot r + e_{1} \\ c_{2} = b \cdot r + e_{2} \\ small \quad r, e_{1}, e_{2} \leftarrow D \\ c_{1}' = a \cdot r' + e_{1}' \\ c_{2}' = b \cdot r' + e_{2}' \\ \hline \bar{c}_{1} = a \cdot \bar{r} + \bar{e}_{1} \\ \bar{c}_{2} = b \cdot \bar{r} + \bar{e}_{2} \\ \hline \hline \bar{c}_{1} = a \cdot \bar{r} + \bar{e}_{1} \\ \bar{c}_{2} = b \cdot \bar{r} + \bar{e}_{2} \\ \hline \hline \bar{c}_{1} = e_{1} + e_{1}' \\ \bar{e}_{1} = e_{1} + e_{1}' \\ \bar{e}_{2} = e_{2} + e_{2}' \\ \hline \end{array}$$

Partial randomized decapsulation

+

• Compute  $c'_1$  and  $c'_2$ , add-then-decrypt  $\bar{c}_1$  and  $\bar{c}_2$ 

## Decrypt with dummy ciphertext (II) 10

- Decrypt<sub>s</sub>(c):  $c_1' = a \cdot r' + e_1'$  $c_2' = b \cdot r' + e_2'$   $r', e_1', e_2' \leftarrow D$ 
  - Compute  $\bar{c}_1 = c_1 + c'_1$  and  $\bar{c}_2 = c_2 + c_2'$

$$\bar{c}_2 - p \cdot \bar{c}_1 \cdot s = p \cdot (e\bar{r} - \bar{e}_1 s) + \bar{e}_2$$

- ⇒ Extract  $\overline{e}_2$ , then  $\overline{r}$ , and then  $\overline{e}_1$ abort if not « 2 × small » recover  $r = \overline{r} - r'$ ,  $e_1 = \overline{e}_1 - e_1'$  and  $e_2 = \overline{e}_2 - e_2'$ abort if not small,  $K = H(r, e_1, e_2)$  and  $c_0 = ADec_K(c_0)$ 
  - Decryption failure issue
    - Not an issue as long as sk = s is small

### Decrypt with dummy ciphertext (II) 10



- Decryption failure issue
  - Not an issue as long as sk = s is small

## Leveling POLKA.dec (I)

\*

leakage-resilience

	SPA	avg-SPA	UP-DPA	DPA
step 1	$egin{aligned} r', e_1', e_2' &\leftarrow \mathcal{D} \ c_1' &= a \cdot r' + e_1' \ c_2' &= a \cdot r' + e_2' \ \overline{c_1} &= c_1 + c_1' \ \overline{c_2} &= c_2 + c_2' \end{aligned}$			
step 2			$t = (p \cdot \overline{c_1}) \cdot s$	
step 3	$egin{aligned} \overline{\mu} = \overline{c_2} - t \ \overline{e_2} &= \overline{\mu}  ext{ mod } p \  ext{if }   \overline{e_2}   > 2B,  ext{ flag } = 1 \ \overline{r} &= (\overline{c_2} - \overline{e_2}) \cdot b^{-1} \  ext{if }   \overline{r}   > 2B,  ext{ flag } = 1 \ \overline{e_1} &= \overline{c_1} - a \cdot \overline{r} \  ext{if }   \overline{e_1}   > 2B,  ext{ flag } = 1 \end{aligned}$			
p 4		$egin{aligned} m{r} &= ar{m{r}} - m{r}' \ egin{aligned}  ext{if} \;   m{r}   &> B, \;  ext{flag} = 1 \ e_1 &= ar{e_1} - e_1' \end{aligned}$		

#### Leveling POLKA.Dec (II)

step 3	$egin{aligned} \overline{e_2} &= \overline{\mu} egin{aligned} &  ext{mod} \ p \ &  ext{if} \   \overline{e_2}   > 2B, \ &  ext{flag} = 1 \ & \overline{r} &= (\overline{c_2} - \overline{e_2}) \cdot b^{-1} \ &  ext{if} \   \overline{r}   > 2B, \ &  ext{flag} = 1 \ & \overline{e_1} = \overline{c_1} - a \cdot \overline{r} \ &  ext{if} \ &   \overline{e_1}   > 2B, \ &  ext{flag} = 1 \end{aligned}$		_		leakage-resilien
step 4		$egin{aligned} r &= \overline{r} - r' \  ext{if} \;   r   > B, \;  ext{flag} = 1 \ e_1 &= \overline{e_1} - e_1' \  ext{if} \;   e_1   > B, \;  ext{flag} = 1 \ e_2 &= \overline{e_2} - e_2' \  ext{if} \;   e_2   > B, \;  ext{flag} = 1 \end{aligned}$			
step 5			$egin{aligned} r^*, e_1^*, e_2^* &\leftarrow \mathcal{D} \  ext{if flag} &= 0 \ K &= H(r, e_1, e_2) \  ext{else} \ K &= H^*(r^*, e_1^*, e_2^*) \end{aligned}$	${f return} M={\sf D}_K(c_0)$	<ul> <li>▲</li> <li>Ieakage-resistance</li> </ul>

#### What remains (leakage-resilience) 13

unknown ephemeral value r

- DPA against  $t = (p \cdot \overline{c_1}) \cdot s$   $\rightarrow$  long-term secret
- + Key-homomorphic (masked with linear overheads)

$$s = s_1 + s_2 + \dots + s_s \Rightarrow t = \sum_{i=1}^d (r \cdot s_i)$$

Norm computations are not key-homomorphic

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# Leveraging physical assumptions?

Very similar to fresh re-keying in symmetric crypto



- Attack path 1: hard physical learning problem
  - Assumed to be hard if L is noisy or algebraically incompatible with *r.s* (formalized as the ring Learning With Physical Rounding problem)

 $\Rightarrow$  It may be sound to unmask  $t = (p \cdot \overline{c_1}) \cdot s$ 

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# Conclusion

- Food for thought (there is a lot to gain)
- Decent instances (e.g., 16-bit q, n = 1024)
- Many important open questions
  - Concrete comparison (e.g., masked Kyber)
    - Challenge: masked Kyber's security?
  - Formalization & reductions
    - Challenge: finer-grain than symmetric crypto
  - Assessing hard physical learning problems?
  - From leakage-resilience to leakage-resistance

(+ other tweaks in the paper: key-homomorphic one-time MAC, implicit vs. explicit rejection)

# THANKS

