

# Using Opinion Dynamics for Probing Cultural Spaces

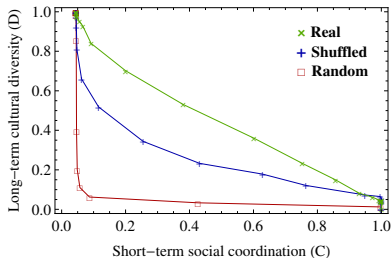
A.I. Babeanu, L. Talman, D. Garlaschelli

Lorentz Institute for Theoretical Physics of Leiden  
University

September 19, 2014



- ▶ compatibility between:
  - ▶ long-term cultural diversity
  - ▶ short-term collective behaviour
- ▶ research questions:
  - ▶ robustness across data sets?
  - ▶ underlying mechanism?
- ▶ important concepts:
  - ▶ cultural space
  - ▶  $D(\omega)$  observable
  - ▶  $C(\omega)$  observable



Valori et al (2012), PNAS **109**: 1068-1073.



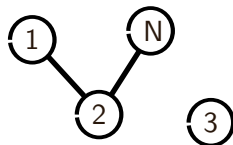
# Cultural space

	$x_1$	$x_2$	$x_3$	$x_N$
$Q_1$ :	A	B	A	C
$Q_2$ :	D	B	B	C
$Q_3$ :	B	A	C	A
$Q_4$ :	A	A	B	E
	$\vdots$	$\vdots$	$\vdots$	$\vdots$
$Q_F$ :	C	A	C	C

	$x_1$	$x_2$	$x_3$	$x_N$
$x_1$	0.0	$d_{12}$	$d_{13}$	$d_{1N}$
$x_2$	$d_{21}$	0.0	$d_{23}$	$d_{2N}$
$x_3$	$d_{31}$	$d_{32}$	0.0	$d_{3N}$
			$\vdots$	
$x_N$	$d_{N1}$	$d_{N2}$	$d_{N3}$	0.0

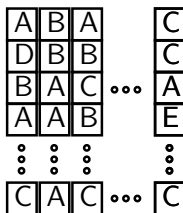
$$d_{ij} > \omega$$

$$d_{ij} = 1 - \frac{1}{F} \sum_{k=1}^F \delta(x_i^k, x_j^k)$$

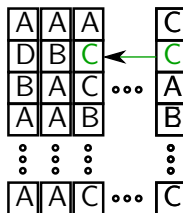


# Long-term cultural diversity $D(\omega)$

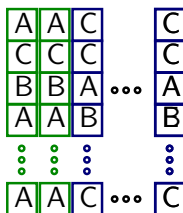
initial



intermediate



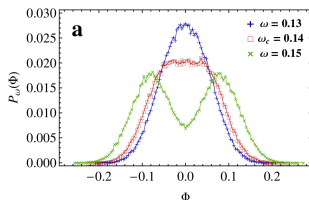
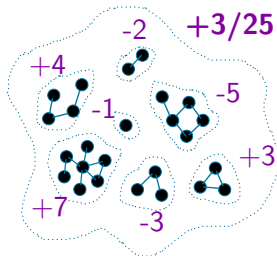
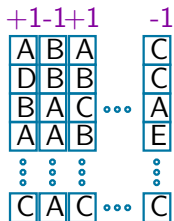
final (absorbing)



$$D(\omega) = \frac{\langle N_D \rangle_\omega}{N}$$



# Short-term collective behaviour $C(\omega)$

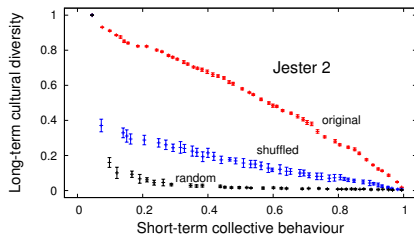
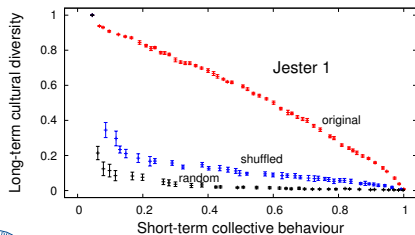
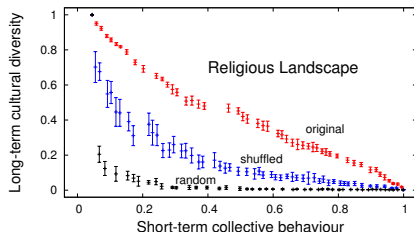
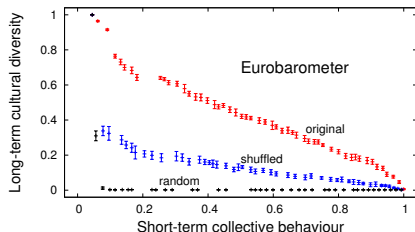


$$C(\omega) = \sqrt{\sum_A \left(\frac{S_A}{N}\right)^2_\omega}$$

Valori et al (2012), PNAS **109**: 1068-1073.

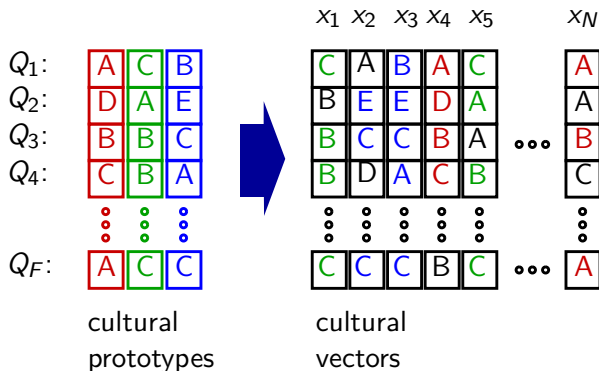


# Robustness across empirical data sets



# Prototype generation

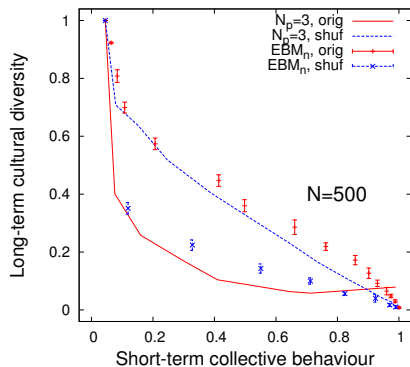
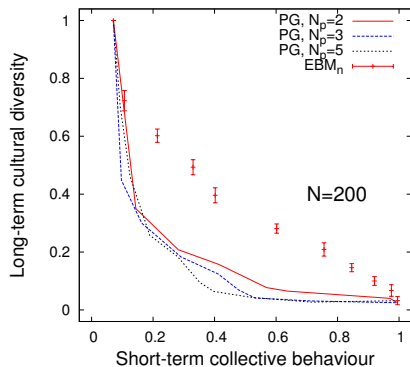
Valid for purely nominal data:



Stivala et al (2014), Sci. Rep. 4:4870.



# Evaluation of prototype generation



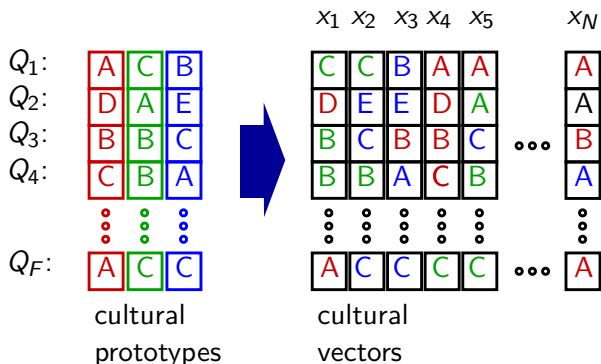
Babeanu et al (2014), in preparation.





# Mixed prototype generation

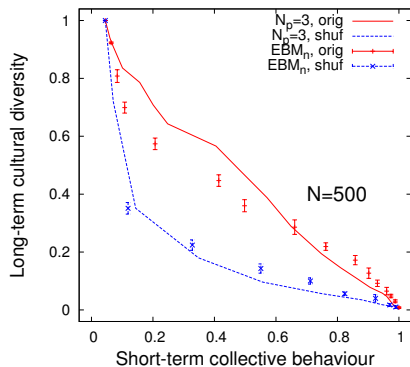
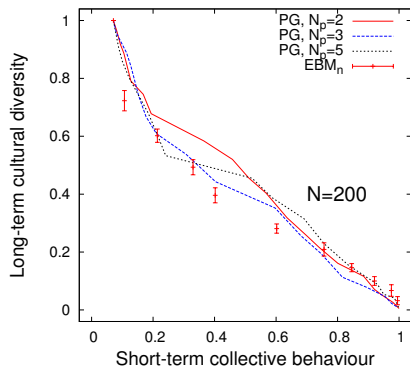
Valid for purely nominal data:



Babeanu et al (2014), in preparation.



# Evaluation of mixed prototype generation

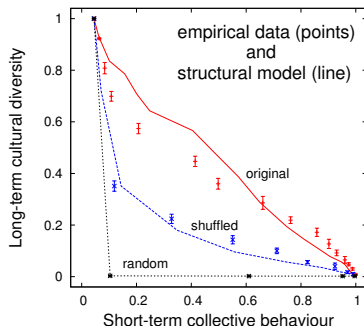


Babeanu et al (2014), in preparation.



# Conclusions

- ▶ results similar across empirical sources
- ▶ “mixed prototypes” hypothesis compatible
- ▶ ! generalize model to ordinal features
- ▶ ! become sensitive to number of prototypes
- ▶ ! more compact, computationally less intensive observables



Babeanu et al (2014), in preparation.

