Errata for Set transformations, symmetrizations and isoperimetric inequalities

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Proof of Lemma 3, p.147 One should replace u_k by u in the second and third lines of the inequality. One should thus read

$$\begin{split} \int_{\mathbf{R}^{2N}} \frac{|u_{k}(y) - u_{k}(x)|^{p}}{|y - x|^{p}} \varrho_{n}(|y - x|) \, dx \, dy \\ \int_{\mathbf{R}^{2N}} \frac{\varrho_{n}(|y - x|)}{|y - x|^{p}} \Big(\int_{\mathbf{R}^{N}} |u(y - z) - u(x - z)| \, \gamma_{k}(z) \, dz \Big)^{p} \, dx \, dy \\ \int_{\mathbf{R}^{2N}} \frac{\varrho_{n}(|y - x|)}{|y - x|^{p}} \Big(\int_{\mathbf{R}^{N}} |u(y - z) - u(x - z)|^{p} \, \gamma_{k}(z) \, dz \Big) \, dx \, dy \\ &= \int_{\mathbf{R}^{N}} \gamma_{k}(z) \Big(\int_{\mathbf{R}^{2N}} \frac{|u(y - z) - u(x - z)|^{p}}{|y - x|^{p}} \varrho_{n}(|y - x|) \, dx \, dy \Big) \, dz \\ &= \int_{\mathbf{R}^{2N}} \frac{|u(y) - u(x)|^{p}}{|y - x|^{p}} \varrho_{n}(|y - x|) \, dx \, dy. \end{split}$$

(Thanks to Almut Burchard for pointing this out.)

Proposition 8, p. 149 The inequality sign should be reversed in the first inequality. One should read

$$F(a,c) + F(b,d) \ge F(a,d) + F(b,c).$$

(Thanks to Augusto Ponce for pointing this out.)

Theorem 3, p. 150 The inequality sign should be reversed in the first inequality. One should read

$$F(a,c) + F(b,d) \ge F(a,d) + F(b,c).$$

(Thanks to Augusto Ponce for pointing this out.)