



Multi-Tuple Leakage Detection and the Dependent Signal Issue

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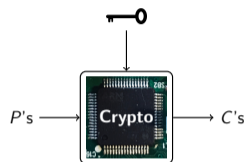
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Leakage Detection

Multi-Tuple Leakage Detection

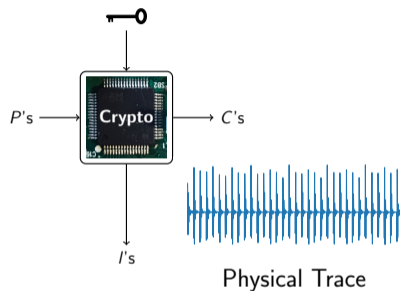
Conclusion

Side-Channel Issue



Encryption on physical devices:

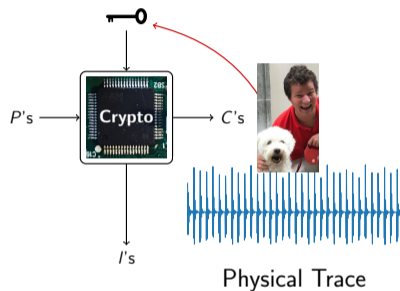
Side-Channel Issue



Encryption on physical devices:

- ▶ With any physical signals

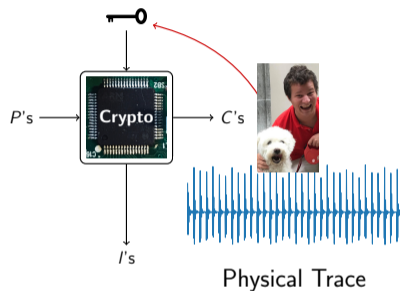
Side-Channel Issue



Encryption on physical devices:

- ▶ With any physical signals
- ▶ Possibly containing secret information

Side-Channel Issue



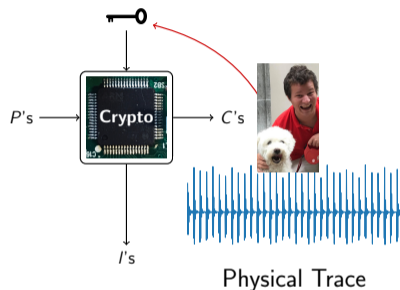
Encryption on physical devices:

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Side-channel Attacks:

- ▶ Known to be hard to prevent
- ▶ Hard to evaluate as well

Side-Channel Issue



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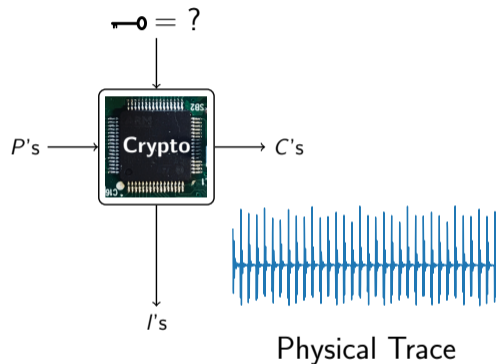
Two evaluation approaches:

- ▶ Attack based
- ▶ Leakage detection

Attack Based Evaluation

Can directly mount attacks:

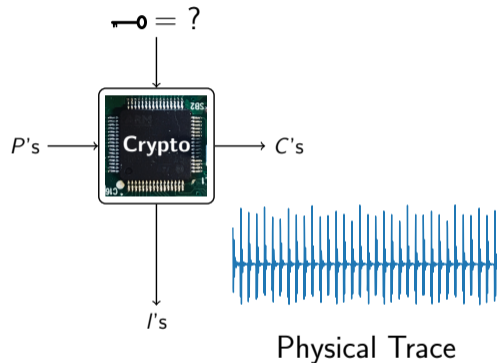
1. Collect measurements



Attack Based Evaluation

Can directly mount attacks:

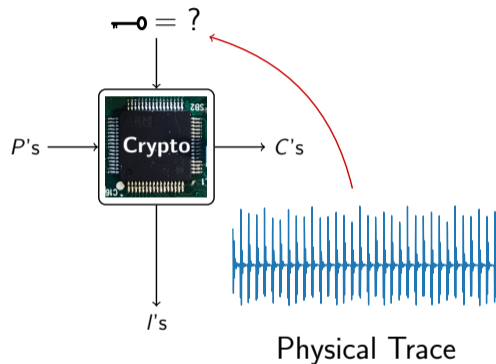
1. Collect measurements
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Attack Based Evaluation

Can directly mount attacks:

1. Collect measurements
2. Perform an attack
3. Retrieve the correct sub-key



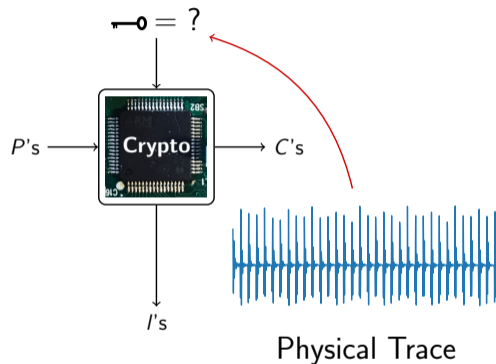
Attack Based Evaluation

Can directly mount attacks:

1. Collect measurements
2. Perform an attack
3. Retrieve the correct sub-key

This requires:

1. Long measurement period
2. Skilled/expert knowledge
3. Distinguish 1 sub-key within 256



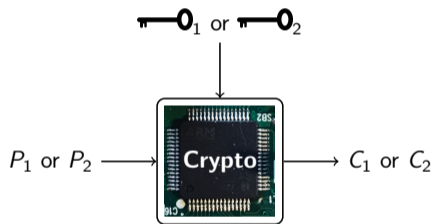
Leakage Detection Based Evaluation

Leakage detection searches for dependency between manipulated data and physical traces.



Leakage Detection Based Evaluation

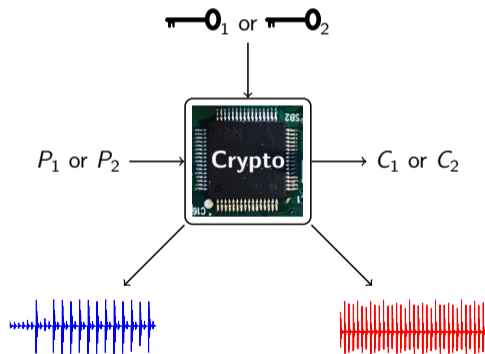
Leakage detection searches for dependency between manipulated data and physical traces.



- ▶ Feed the core with two different sets of inputs

Leakage Detection Based Evaluation

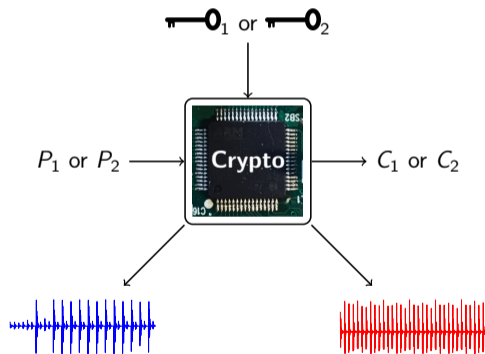
Leakage detection searches for dependency between manipulated data and physical traces.



- ▶ Feed the core with two different sets of inputs
- ▶ Record the corresponding traces

Leakage Detection Based Evaluation

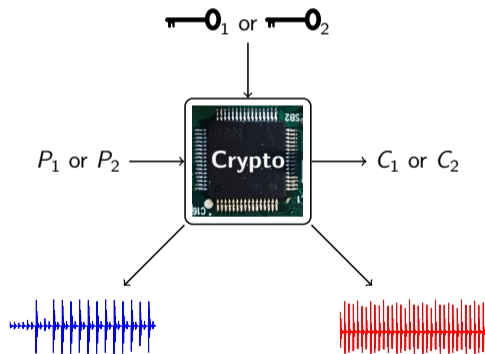
Leakage detection searches for dependency between manipulated data and physical traces.



- ▶ Feed the core with two different sets of inputs
- ▶ Record the corresponding traces
- ▶ Observe differences between the two sets

Leakage Detection Based Evaluation

Leakage detection searches for dependency between manipulated data and physical traces.

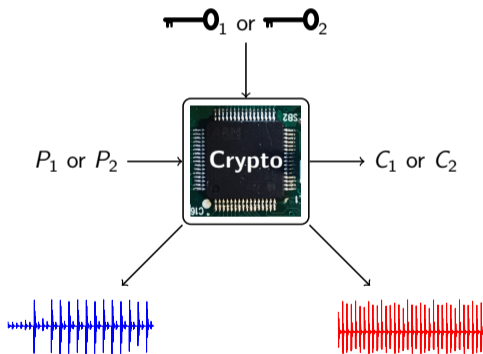


How does it compare with attack based evaluations:

- ▶ Shortened measurement period (Possibly)
- ▶ No skilled/expert knowledge

Leakage Detection Based Evaluation

Leakage detection searches for dependency between manipulated data and physical traces.



How does it compare with attack based evaluations:

- ▶ Shortened measurement period (Possibly)
- ▶ No skilled/expert knowledge

A good first check but:

- ▶ Risk of false positives and false negatives

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Leakage Detection

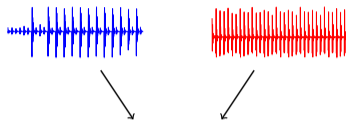
Find a difference between the two sets:



Leakage Detection

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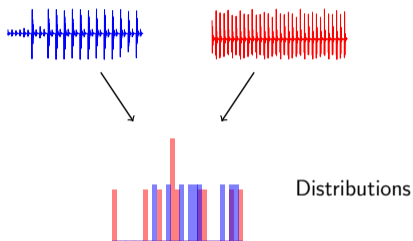
1. Select a point in time



Leakage Detection

Find a difference between the two sets:

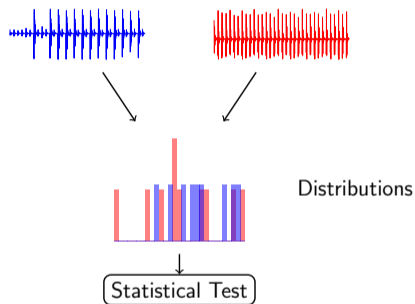
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2. Record traces to observe a distribution



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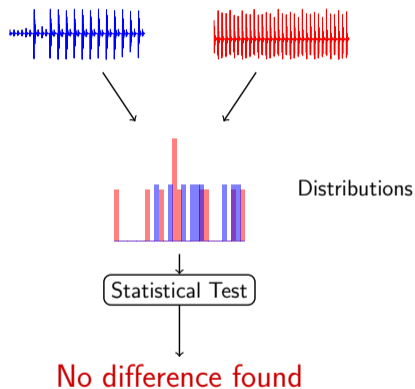
1. Select a point in time
2. Record traces to observe a distribution
3. Perform a statistical test



Leakage Detection

Find a difference between the two sets:

1. Select a point in time
2. Record traces to observe a distribution
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4. Observe its binary output

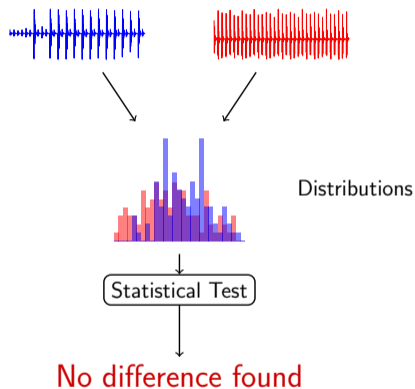


Leakage Detection

Find a difference between the two sets:

1. Select a point in time
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Repeat with more measurements if needed

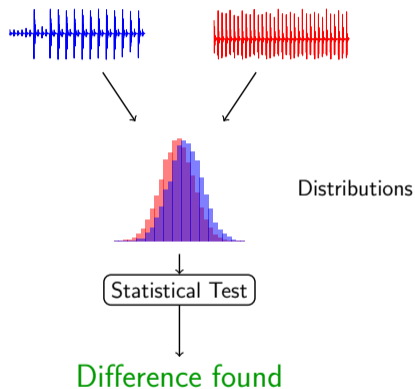


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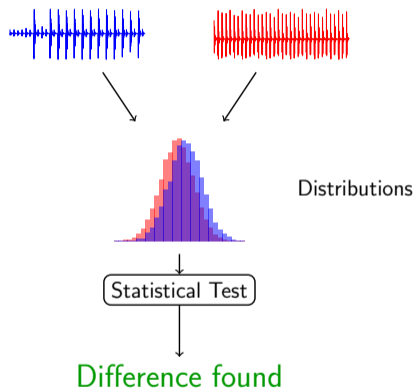
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The statistical test can search for difference in:

- ▶ Means with the Welch's t -test
- ▶ Distributions with χ^2 -test
- ▶ ...



Leakage Detection

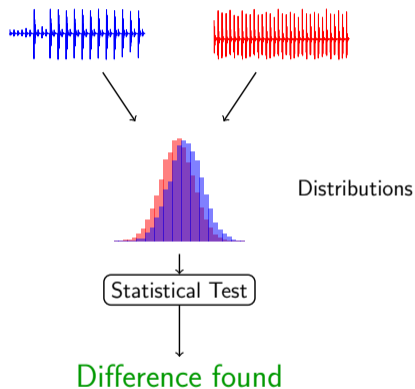
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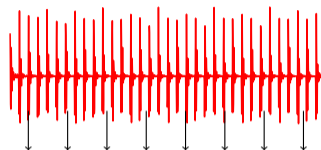
- ▶ Means with the Welch's t -test \implies **Most popular**
- ▶ Distributions with χ^2 -test
- ▶ ...



Leakage Detection: TVLA

The traces contain multiple points in time:

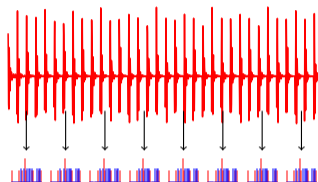
1. Select **all** the points in time



Leakage Detection: TVLA

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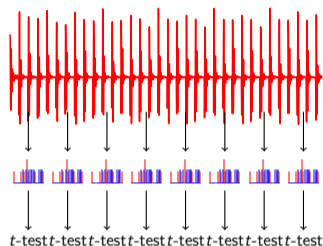
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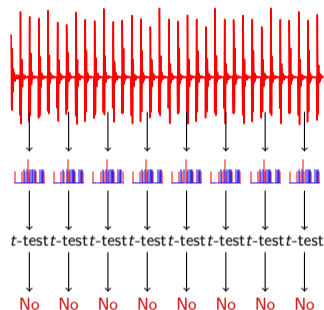
1. Select **all** the points in time
2. Record traces to observe a distribution
3. Perform **independent** statistical test



Leakage Detection: TVLA

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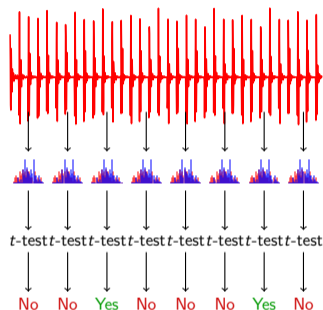
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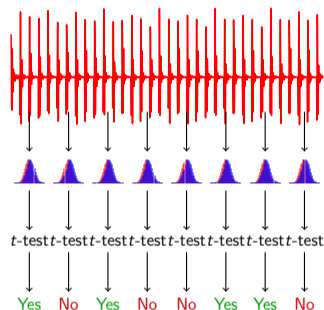
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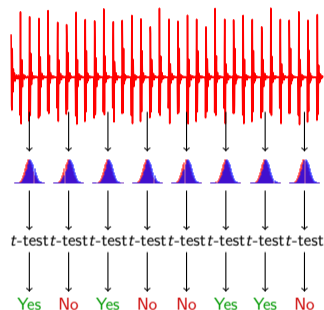
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Difference found if:

- ▶ At least one of the tests goes above a threshold



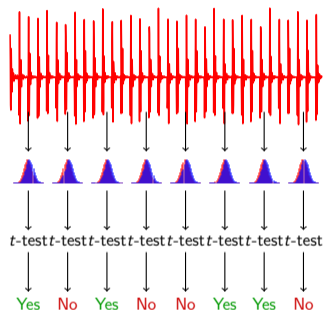
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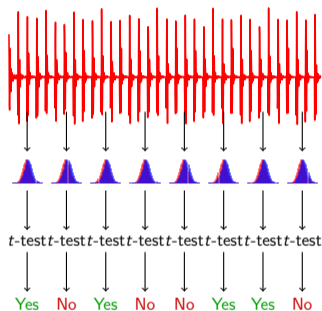
1. Select **all** the points in time
2. Record traces to observe a distribution
3. Perform **independent** statistical test
4. Observe their binary outputs

Difference found if:

- ▶ At least one of the tests goes above a threshold
- ▶ Selected thanks to:
 - ▶ Desired confidence
 - ▶ Number of considered time samples
 - ▶ Assuming independence between them

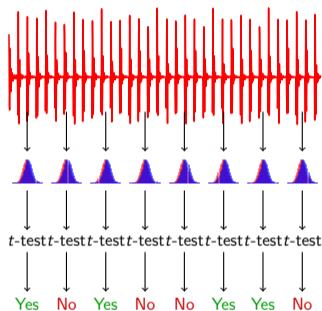


Limitations to TVLA



TVLA performs independent t -test:

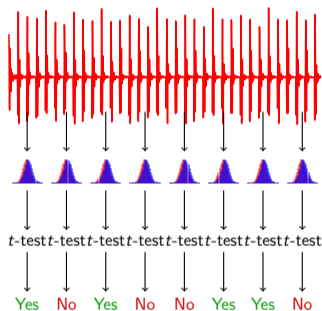
Limitations to TVLA



TVLA performs independent t -test:

- Impossible to take advantage of multivariate leakage

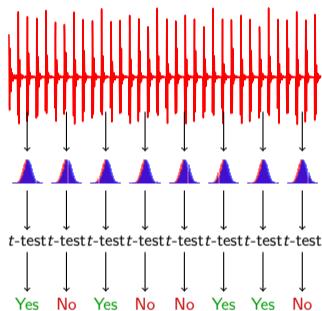
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- ▶ Could lead to reduced measurement period

Limitations to TVLA

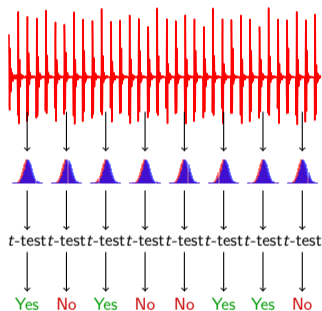


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Independence in the signal is usually not met:

Limitations to TVLA



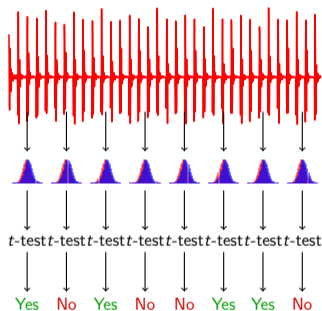
TVLA performs independent t -test:

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Independence in the signal is usually not met:

- ▶ Wrong assumption while setting the threshold

Limitations to TVLA



TVLA performs independent t -test:

- ▶ Impossible to take advantage of multivariate leakage
- ▶ Could lead to reduced measurement period

Independence in the signal is usually not met:

- ▶ Wrong assumption while setting the threshold
 - ▶ Hard to interpret results (especially negative ones)

Content

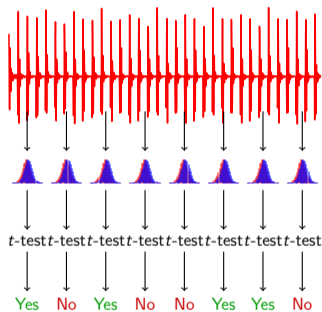
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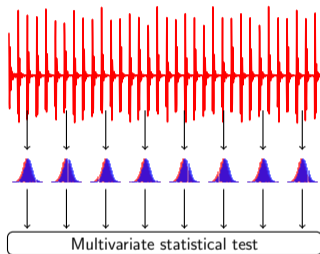
Conclusion

Multi-Tuple Leakage Detection: General Idea



Approach:

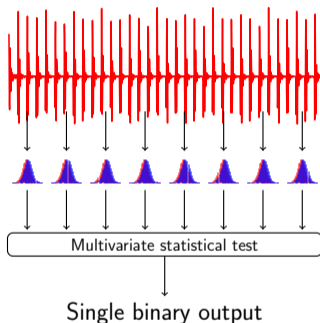
Multi-Tuple Leakage Detection: General Idea



Approach:

- Replace the independent tests by a single one

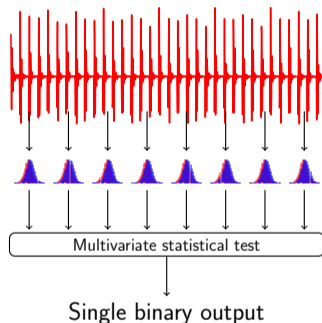
Multi-Tuple Leakage Detection: General Idea



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Multi-Tuple Leakage Detection: General Idea



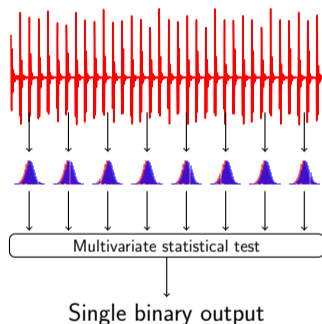
Approach:

- ▶ Replace the independent tests by a single one

Natural candidate: Hotelling's T^2 -test

- ▶ Do not assume independence
- ▶ Need to invert a covariance matrix
- ▶ Not always applicable

Multi-Tuple Leakage Detection: General Idea



Approach:

- ▶ Replace the independent tests by a single one

Natural candidate: Hotelling's T^2 -test

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- ▶ Need to invert a covariance matrix
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Heuristic alternative: D -test

- ▶ Assume independence
 - ▶ Hard to interpret results

Traces Parameter: Density

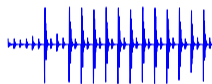
Density of informative points:

- ▶ The proportion of leaking points
- ▶ t -test showing difference with ∞ of measurements

Traces Parameter: Density

Density of informative points:

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↓
 t -test
↓

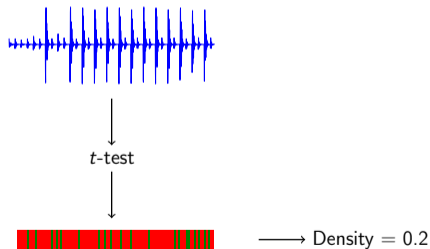


→ Density = 0.1

Traces Parameter: Density

Density of informative points:

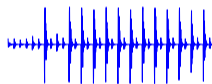
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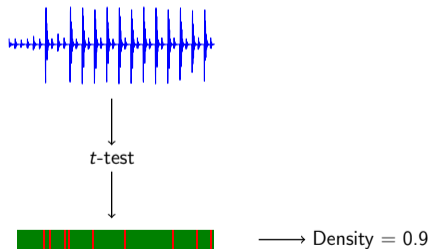


→ Density = 0.5

Traces Parameter: Density

Density of informative points:

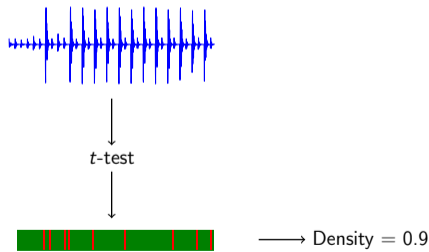
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Traces Parameter: Density

Density of informative points:

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Typical settings:

- ▶ Protected software: low density, long traces
- ▶ Hardware unprotected: high density, short traces

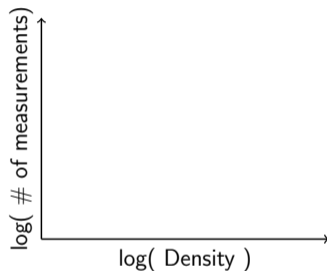
Multi-Tuple Leakage Detection: Features

From simulations with fixed trace length:

—————→
log(Density)

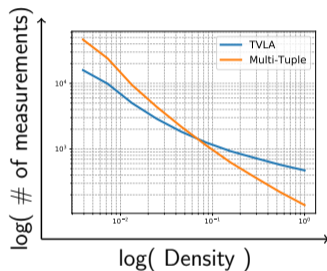
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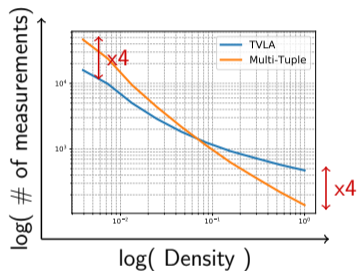
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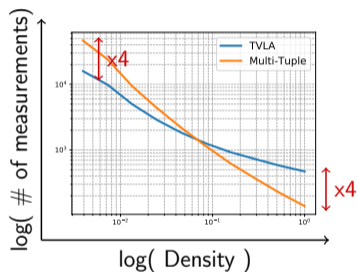
- ▶ Both methods suffer from a low density



Multi-Tuple Leakage Detection: Features

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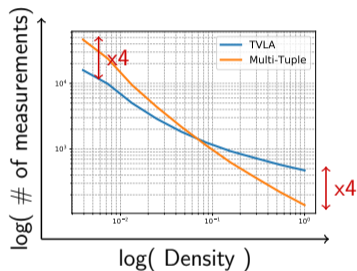
- ▶ Both methods suffer from a low density
- ▶ Multi-Tuple more than the TVLA



Multi-Tuple Leakage Detection: Features

From simulations with fixed trace length:

- ▶ Both methods suffer from a low density
- ▶ Multi-Tuple more than the TVLA



Reduced data complexity with **higher density**

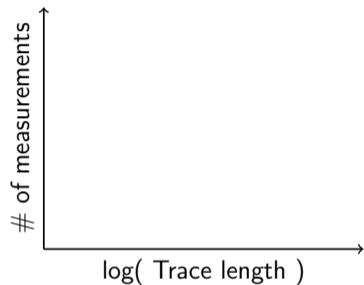
Multi-Tuple Leakage Detection: Parameters

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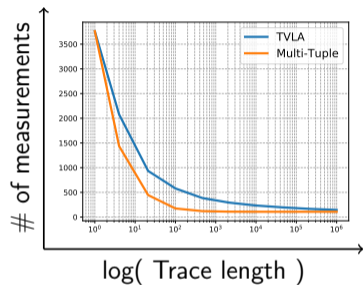
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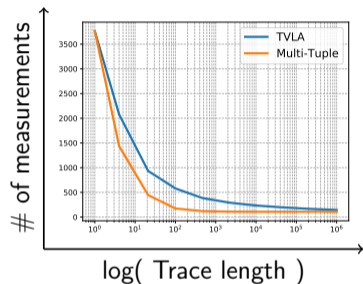
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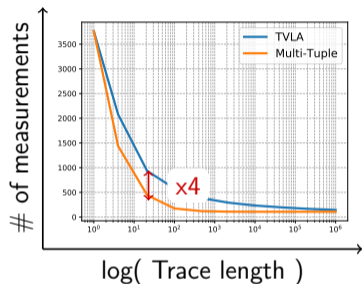
- ▶ Both methods take advantage of longer traces



Multi-Tuple Leakage Detection: Parameters

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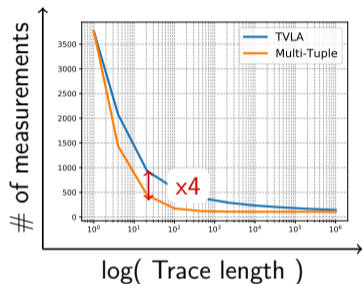
- ▶ Both methods take advantage of longer traces
- ▶ Multi-Tuple gains more than the TVLA



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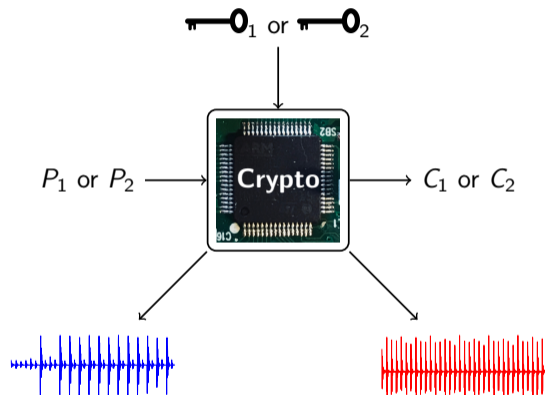
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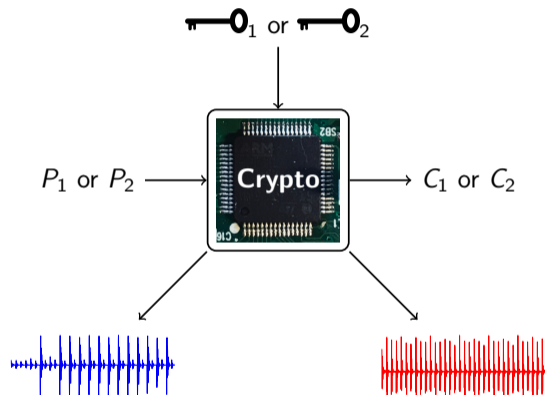
- ▶ Reduced data complexity with the **number of time samples**
- ▶ The jointly processed trace size is limited for Hotelling's test because of covariance matrix inversion (~ 2000):
 - ▶ Possibility to run multiple Hotelling's tests in parallel

Practical Evaluation Scenarios



Two extreme settings:

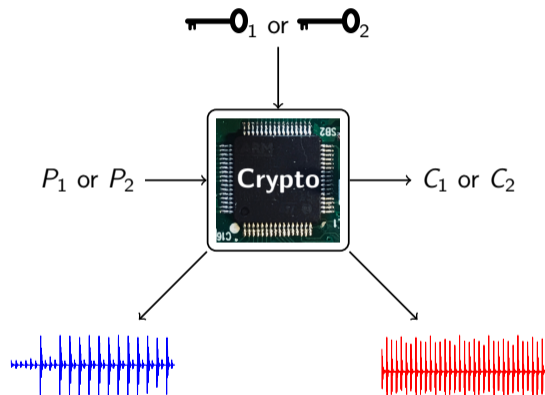
Practical Evaluation Scenarios



Two extreme settings:

- ▶ White Box: everything is known about the design

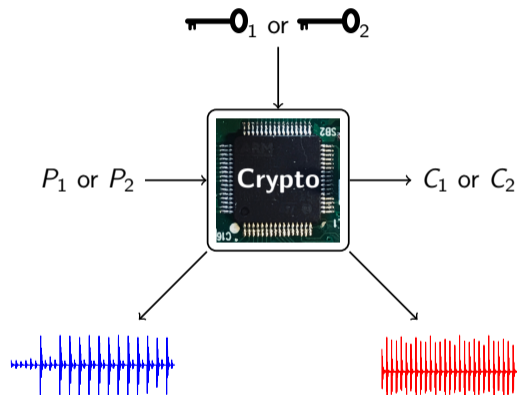
Practical Evaluation Scenarios



Two extreme settings:

- ▶ White Box: everything is known about the design
- ▶ Black Box: nothing is known about the design

Practical Evaluation Scenarios



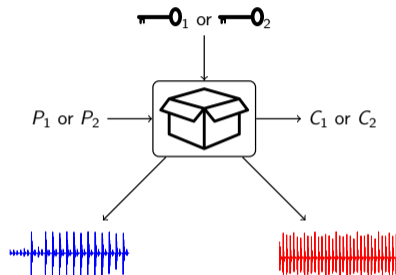
Two extreme settings:

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How to perform Leakage Detection in these settings ?

Practical Evaluation Scenarios: White Box

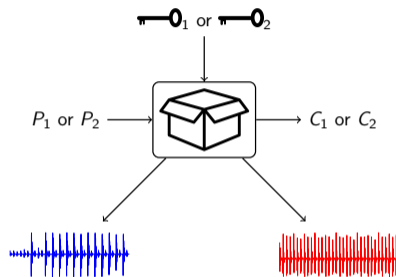
In White Box:



Practical Evaluation Scenarios: White Box

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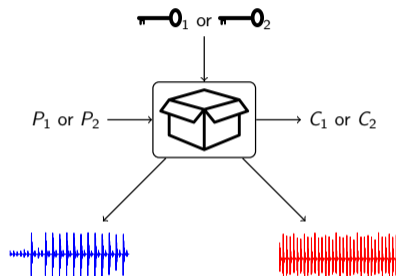
- ▶ Prior information about leaking points



Practical Evaluation Scenarios: White Box

In White Box:

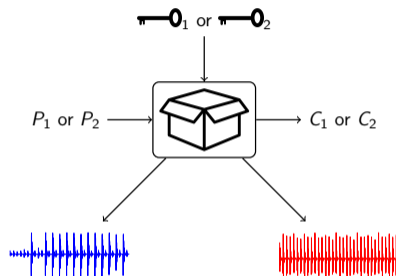
- ▶ Prior information about leaking points
 - ▶ Can reduce traces



Practical Evaluation Scenarios: White Box

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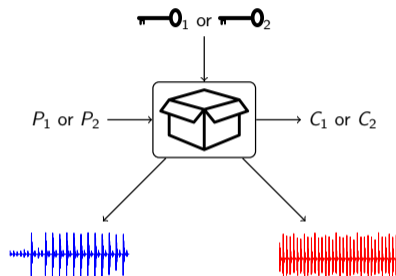
- ▶ Prior information about leaking points
 - ▶ Can reduce traces
 - ▶ Can invert the covariance matrix (Hotelling's T^2 -test)
 - ▶ High density



Practical Evaluation Scenarios: White Box

In White Box:

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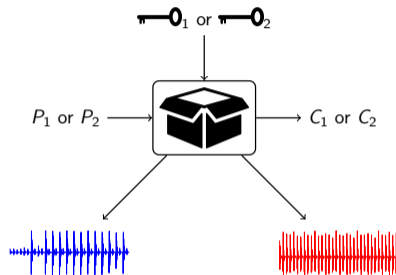


As a result:

- ▶ Smaller measurement period
- ▶ Easy interpretation of the confidence (no \perp assumption)

Practical Evaluation Scenarios: Black Box

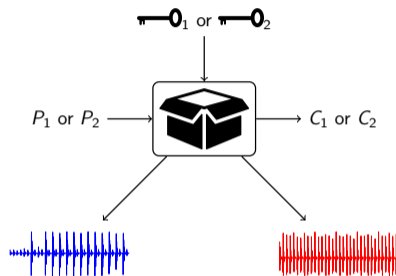
In Black Box:



Practical Evaluation Scenarios: Black Box

In Black Box:

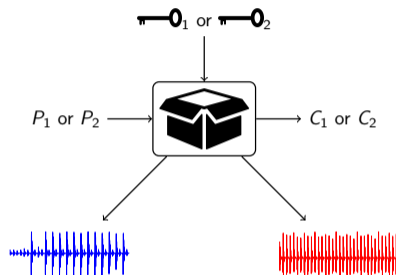
- ▶ No prior information about leaking points



Practical Evaluation Scenarios: Black Box

In Black Box:

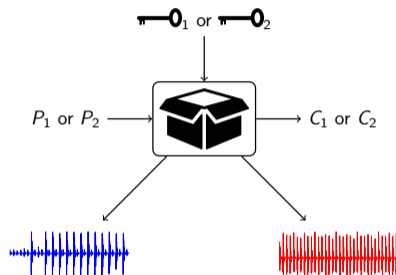
- ▶ No prior information about leaking points
 - ▶ Can't reduce traces



Practical Evaluation Scenarios: Black Box

In Black Box:

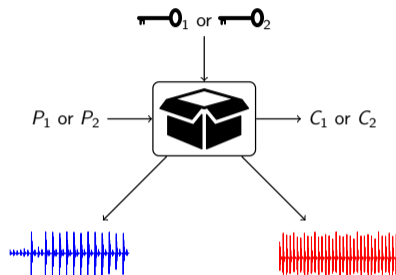
- ▶ No prior information about leaking points
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 - ▶ Can't always invert the covariance matrix



Practical Evaluation Scenarios: Black Box

In Black Box:

- ▶ No prior information about leaking points
 - ▶ Can't reduce traces
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 - ▶ Fixed density



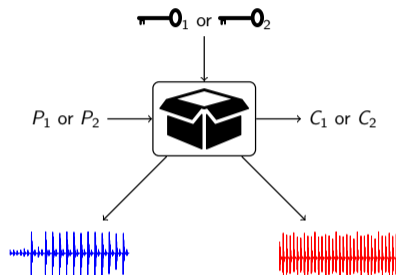
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As a result:

- ▶ Possibly larger measurement period



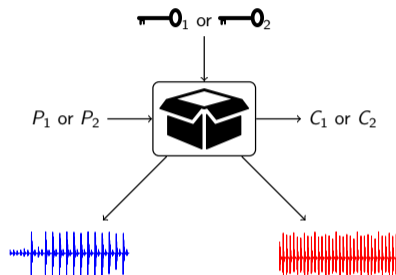
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As a result:

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- ▶ Independent assumption needed



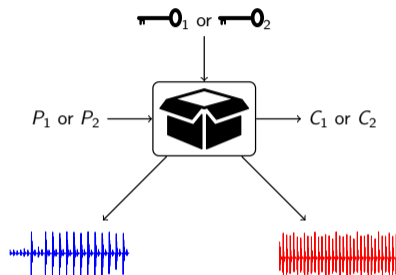
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As a result:

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- ▶ Independent assumption needed
 - ▶ Heuristic required for confidence level interpretation:
 - ▶ TVLA: too conservative
 - ▶ D -test: too optimistic



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 - ▶ And sometimes reduction the measurement period
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Thanks !



Evaluation Hardness

github.com/obronchain/multiple_leakage_detection